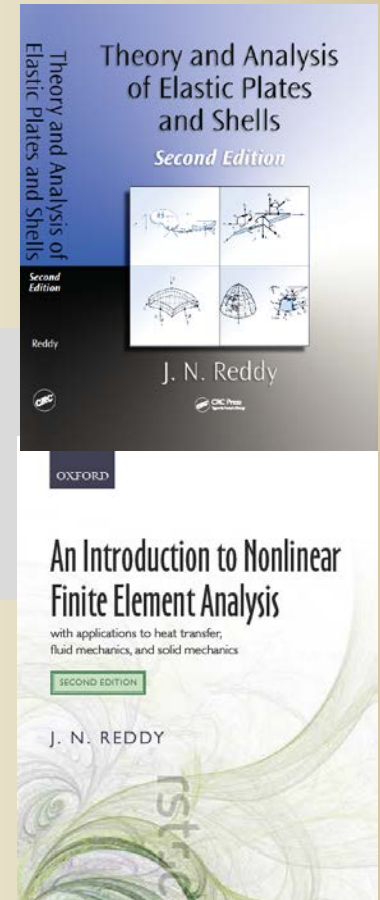


THEORY AND ANALYSIS OF LAMINATED COMPOSITE AND FUNCTIONALLY GRADED BEAMS, PLATES, AND SHELLS



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* This document contains a copy of the overheads used in the course. Much of the material used in the course comes from the instructor's book, *Mechanics of Laminated Composite Plates and Shells* (2nd ed., CRC Press, 2004); other material comes from the research publications of the lecturer.



THEORY AND ANALYSIS OF LAMINATED COMPOSITE AND FUNCTIONALLY GRADED BEAMS AND PLATES

CONTENTS

- **Composite Materials: General Introduction**
- **Laminate Theories (CLPT and FSDT)**
- **Finite Element Models**
- **FGM Beams and Plates**

- **Nonlocal Elasticity of Eringen for Beams**
- **Modified Couple Stress Theory of Beams and Plates**
- **Strain Gradient Theory of Srinivasa and Reddy**
- **Summary of the Course and Closing Comments**



COMPOSITE MATERIALS: General Introduction

- **Composite Materials - Definition**
- **The Big Picture**
- **The Role of Stress Analysis**
- **Classification of Composites**
- **Advantages and Disadvantages of Composites**
- **Use of Composite Materials in Aerospace Structures**
- **Study Areas in Composites**
- **Structural Analysis of Composite Structures**
- **Mechanical Characterization**

NOTE:

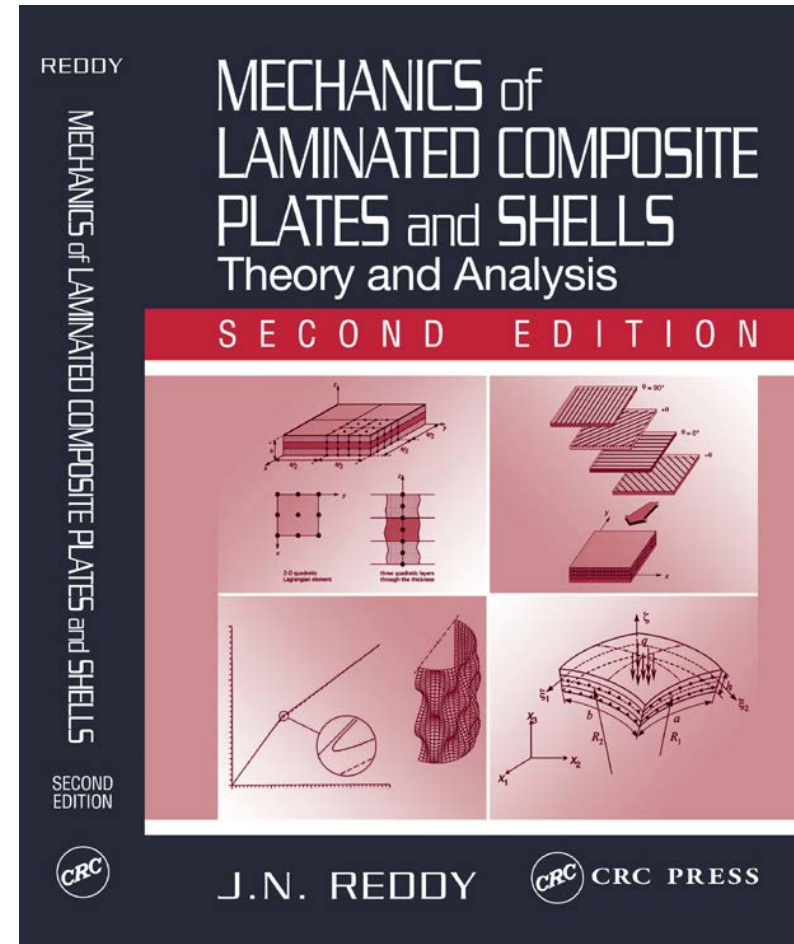
Minor changes are made here and there to the viewgraphs without adding any major new material.

PRIMARY REFERENCE

on mechanics of composite materials

J. N. Reddy, *Mechanics of Laminated Composite Plates and Shells*, 2nd ed., CRC Press, 2004 (introduction to the theory and analysis - analytical as well as FEM - of laminated composite plates and shells)

A list of papers authored by JN Reddy is provided at the end of this lecture notes. References to the works of many other authors can be found in *References* cited in the author's papers.



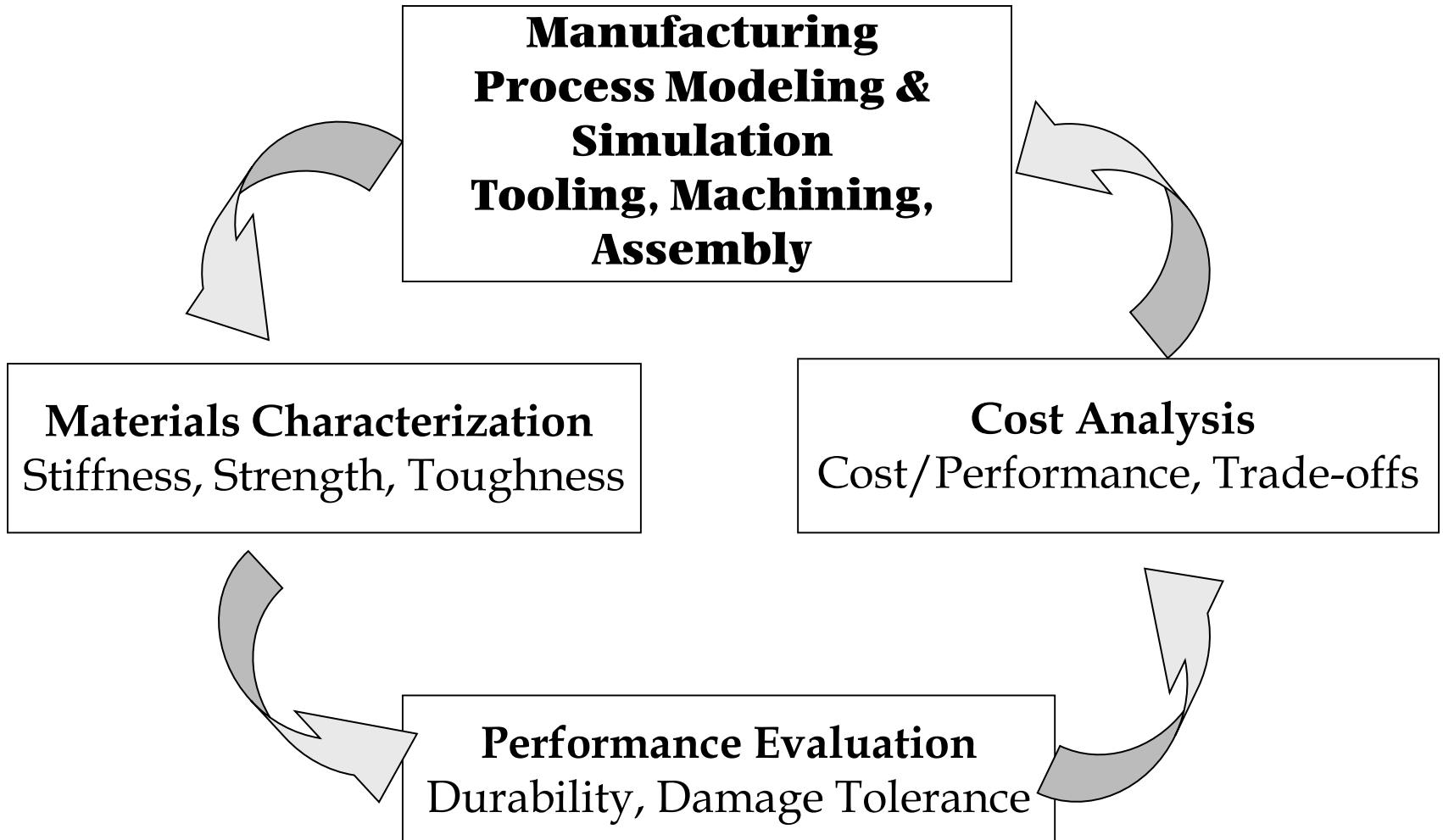


COMPOSITE MATERIALS-Definition

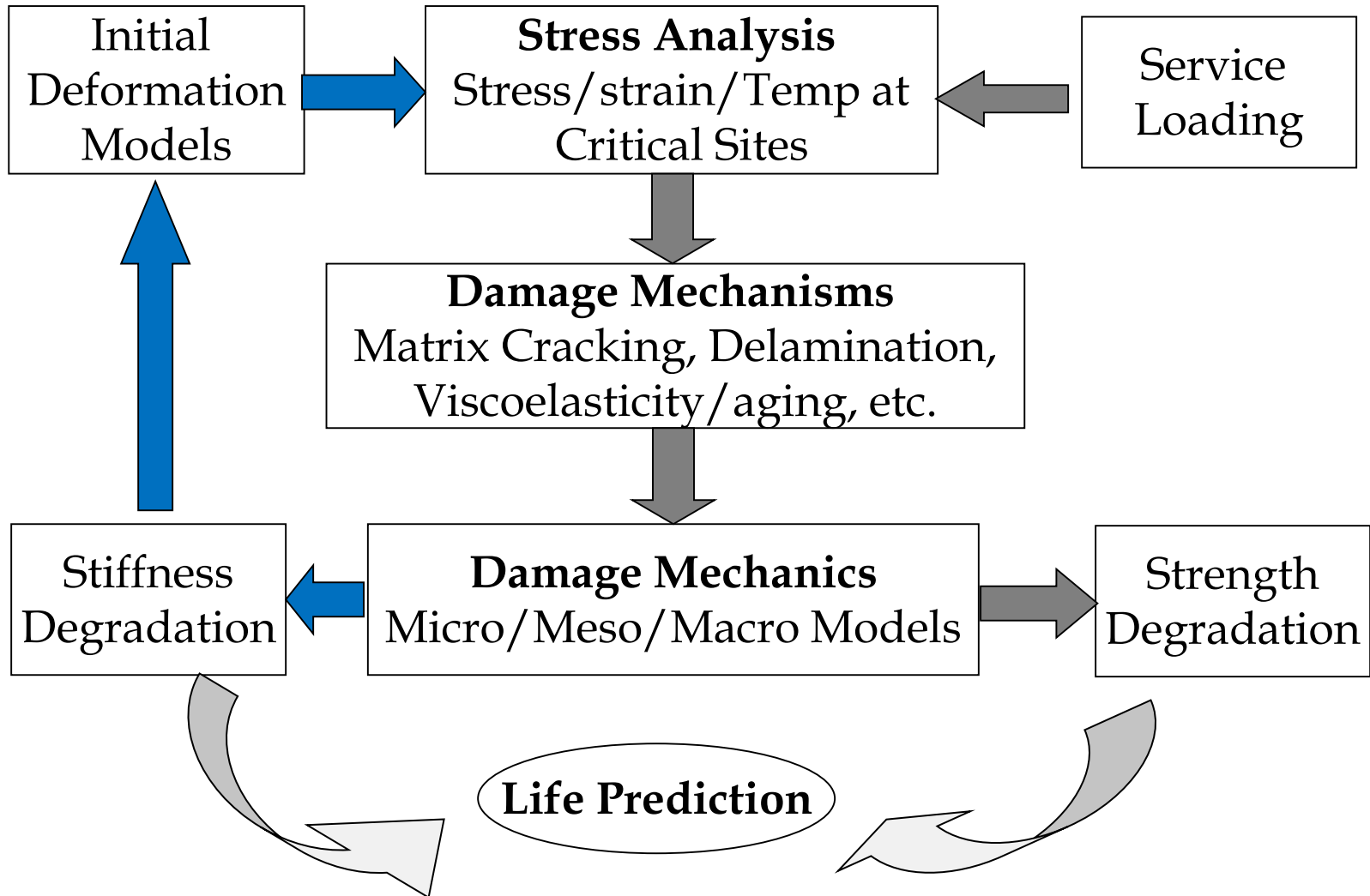
Definition: Two or more materials combined on a *macroscopic* scale to form a useful third material

Properties to be Improved: Strength, stiffness, weight, fatigue life, wear resistance, thermal insulation, thermal conductivity, corrosion resistance, acoustical insulation, etc.

THE BIG PICTURE



THE ROLE OF STRESS ANALYSIS





CLASSIFICATION OF COMPOSITE MATERIALS

- Fibrous composites:*** Fibers in a matrix
- Particulate composites:*** Particles in a matrix
- Combinations of above:*** Reinforced fiber-reinforced composites
- Woven composites***
- Braided composites***
- Laminated composites:*** Layers of various materials (nano-composites)

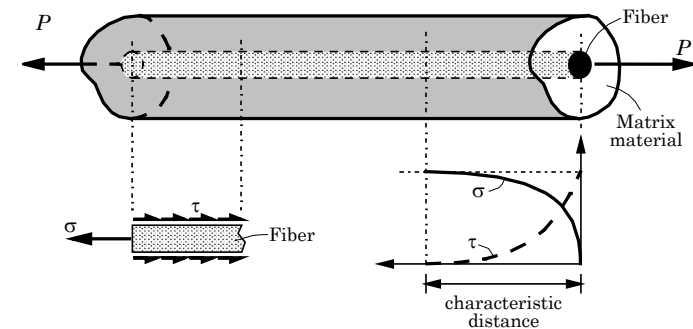
Fiber-reinforced Composite

Materials: Constituents

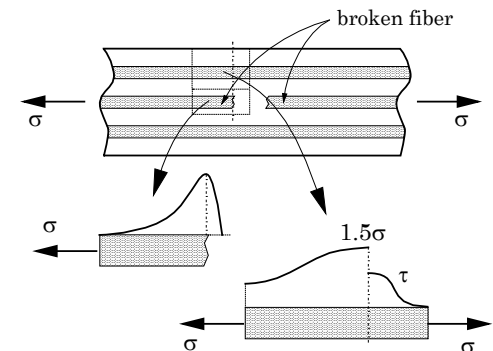
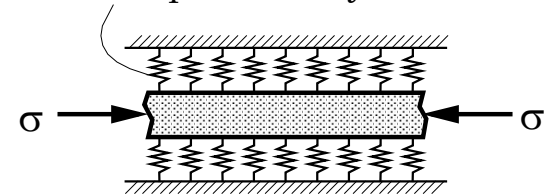
Fiber: Load-carrying agent

Matrix: Supports and protects fibers, and transfers load between broken fibers

Lamina: Basic building block; flat or curved arrangement of unidirectional or woven fibers in a matrix

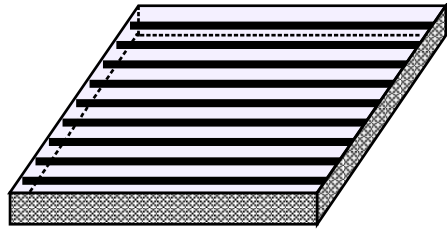


springs represent the lateral restraint provided by the matrix

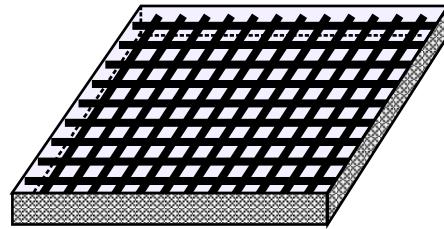


(c)

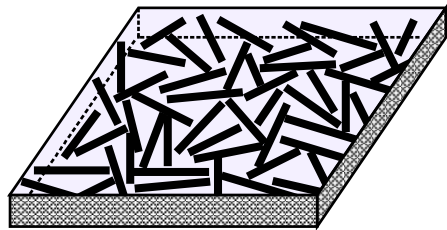
Classification of Composite Materials



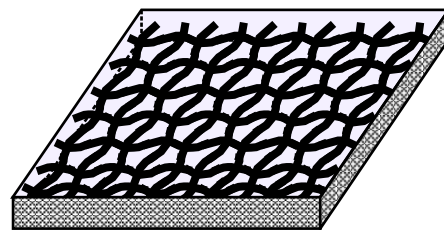
(a) Unidirectional



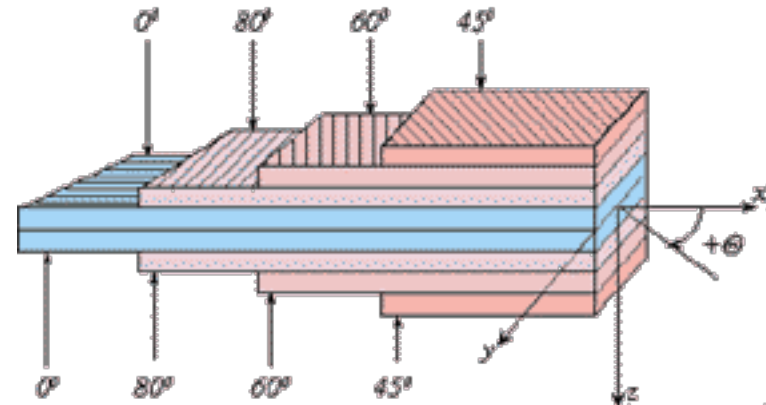
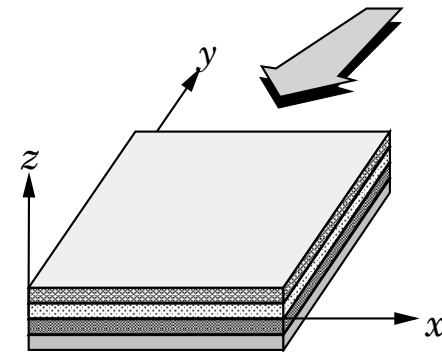
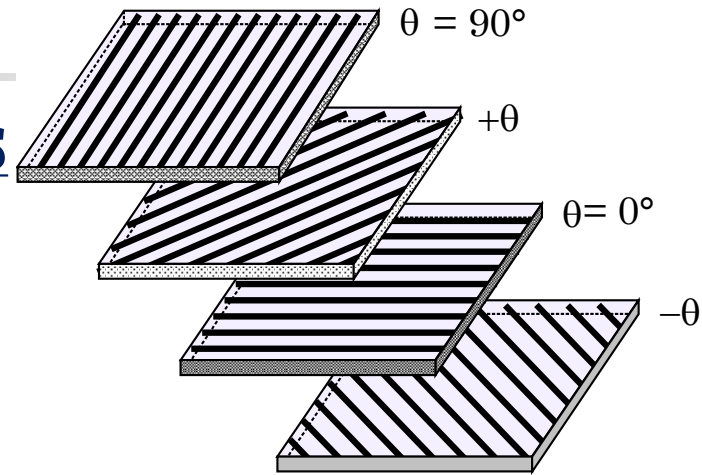
(b) Bi-directional



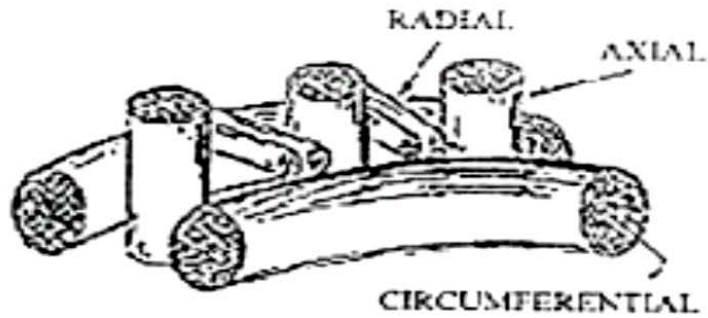
(c) Discontinuous fiber



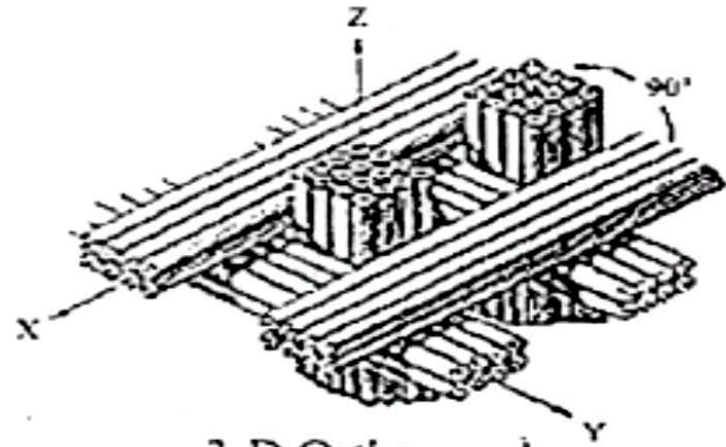
(d) Woven



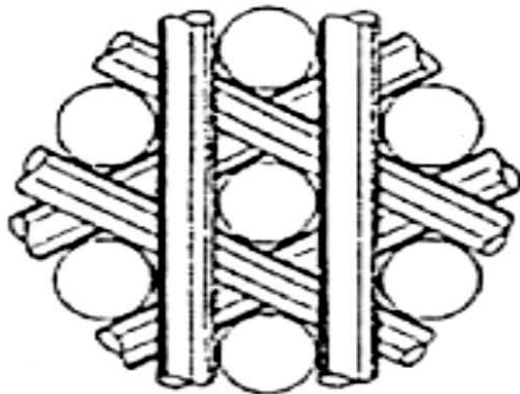
Woven Composites



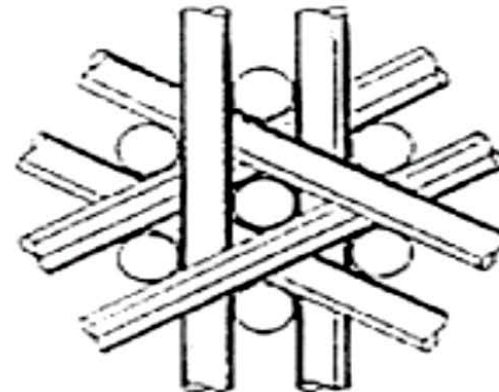
3-D Cylindrical



3-D Orthogonal



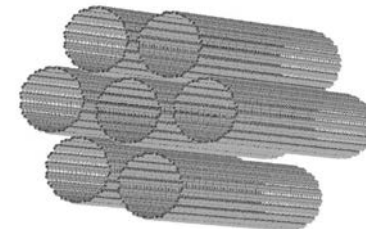
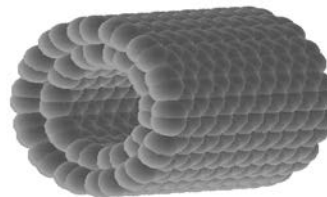
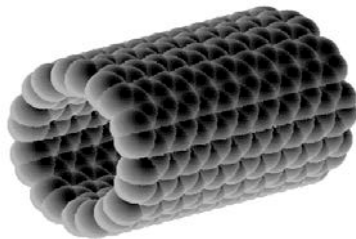
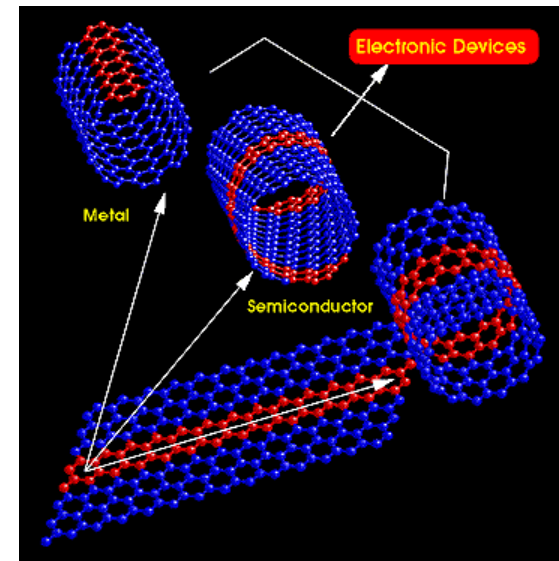
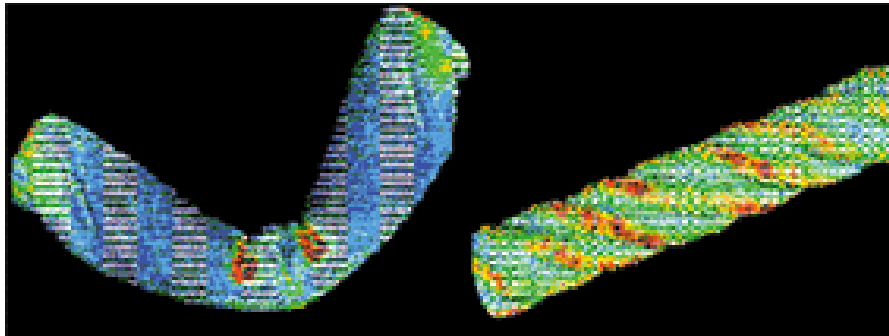
4-D In-Plane



4-D Pyramidal

Nanocomposites: Carbon Nanotubes

Carbon nanotubes can be viewed as a sheet of graphite that has been rolled in to a single tube. Carbon nanotubes can be single- or multi-walled.

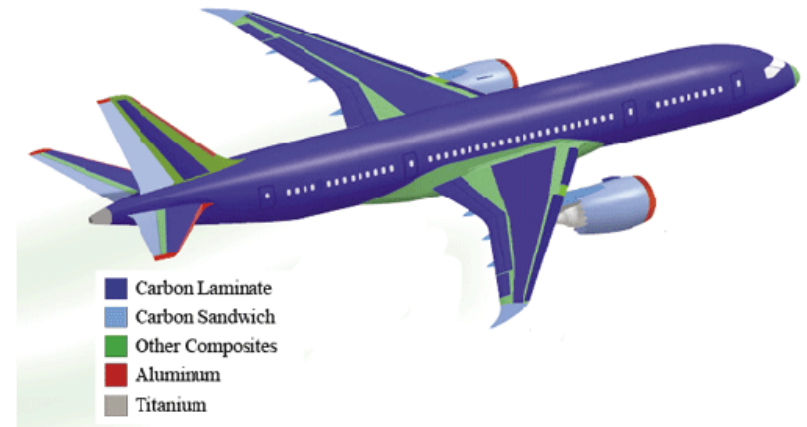


Advantages/Disadvantages of Composites

| <i>Advantages</i> | <i>Disadvantages</i> |
|---|--|
| <ul style="list-style-type: none">• Weight reduction• High strength or stiffness to weight ratio• Tailorable properties• Can tailor strength or stiffness in the load direction• Longer life (no corrosion)• Lower manufacturing costs because of less part count.• Inherent damping.• Increased (or decreased) thermal or electrical conductivity | <ul style="list-style-type: none">• Cost of raw material and fabrication• Transverse properties may be weak.• Matrix is weak, low toughness• Reuse and disposal may be difficult• Difficult to attach.• Analysis is difficult.• Matrix subjected to environment degradation. |

Composites in Aerospace Structures

Boeing 787 – more than 50% structure is made of composites



Composite components are approximately 15% of structural weight for civil aircraft.

For military aircrafts and helicopters, it is 40% of structural weight.

Earlier use of fibrous composites in aerospace are because of the potential for lighter structures as it affects fuel consumption, performance, and payload



Design requirements and objective for aerospace vehicles

| Product | Structural item | Primary structural requirements | Primary design Objectives |
|--------------------------|------------------------|--|--|
| <u>Aircraft</u> | Airframe | Compressive strength Damage tolerance Joint strength Durability | Minimum weight Maximum service |
| | Rotor blades | Tensile strength Stiffness Fatigue life | Minimum weight Maximum service life |
| <u>Helicopter</u> | Understructure | Stiffness Energy absorption | Minimum weight Crashworthiness |

Design requirements and objective for aerospace and underwater vehicles

| Product | Structural item | Primary structural requirements | Primary design Objectives |
|------------------------|------------------------|--|---|
| Rocket motor | Motor cases nozzles | Tensile strength Resistance to elevated temperature | Minimum weight Survivability at 2000 C |
| Satellite | Rotor blades | Stiffness Low thermal expansion | Minimum weight Dimensional stability |
| Marine (sub-mercibles) | Understructure | Compression strength and stability Joint integrity | Minimum weight Maximum depth |

CHOICE OF COMPOSITE MATERIALS

| Reason for use | Material selected | Application/driver |
|-----------------------------------|--|---|
| Lower inertia, less deflection | High strength carbon/graphite-epoxy | Industrial rolls |
| Light weight, damage tolerance | High strength carbon/graphite, hybrids, epoxy | Trucks and buses to reduce environment pollutions |
| More reproducible complex surface | High strength or high modulus carbon, graphite epoxy | High special aircraft |